Design, Synthesis, and Characterization of a High-Affinity Trivalent System Derived from Vancomycin and L-Lys-d-Ala-d-Ala

Jianghong Rao, Joydeep Lahiri, Robert M. Weis,* and George M. Whitesides*

Contribution from the Department of Chemistry and Chemical Biology, Harvard University, 12 Oxford Street, Cambridge, Massachusetts 02138

Received July 26, 1999

Abstract: A trivalent derivative of vancomycin, tris(vancomycin carboxamide), \([\text{C}_6\text{H}_3\text{N}[\text{CONH}\text{C}_2\text{H}_4\text{H}_2\text{C}_2\text{H}}\text{NCONH}])_3 (\text{R}_3\text{V}_3\text{V} = \text{vancomycin})\), binds an analogous trivalent derivative of d-Ala-d-Ala, R_3L_3, (\text{C}_6\text{H}_3\text{N}[\text{CONH}N\text{Ac}])_3\text{L}_3-d\text{-Ala-d-Ala}) in water with a dissociation constant that is approximately \(4 \times 10^{-17}\) M, as estimated by HPLC using a competitive assay against N\text{Ac}-d\text{-Ala-d-Ala-d-Ala} (L). This binding is one of the tightest known for low molecular weight organic species. The dissociation of \(R_3V_3; R'_3L'_3\) in the presence of an excess of L could be followed by HPLC. The kinetics of dissociation are quite different from those of monovalent tight-binding systems such as avidin and biotin. In particular, the rate of dissociation of the aggregate \(R_3V_3; R'_3L'_3\) is rapid in the presence of monovalent L at concentrations greater than the value of the dissociation constant for the complex of L with V; by contrast, the rate of dissociation of biotin-avidin is independent of the concentration of biotin. Two mechanisms by which the dissociation may occur are postulated and discussed. Calorimetric measurements for the trivalent system indicate that the enthalpy of association is \(~40\) kcal/mol, about three times that of \(V + L\), and thus the entropy of association is \(~18\) kcal/mol, approximately 4.5 times that of \(V + L\).

Introduction

We are developing vancomycin (V) and d-Ala-d-Ala (DADA) as a model system with which to study the physical-organic chemistry and physical biochemistry of polyvalency.\(^1\)\(^2\) Vancomycin binds to peptides terminating in d-Ala-d-Ala with dissociation constants ranging from about 100 \(\mu\)M for (N-acetyl-d-Ala-d-Ala) to about 1 \(\mu\)M for (d-Ala-l-Lys-d-Ala-d-Ala and similar compounds).\(^3\)\(^4\) The geometry of these complexes is well-defined (Scheme 1),\(^5\)\(^6\) and similar compounds.\(^3\)\(^4\) Vancomycin is rigid, and the values of thermodynamic parameters for its association with N-acetyl-d-Ala-d-Ala (at 298 K, \(\Delta G^0 = -5.2\) kcal/mol; \(\Delta H^0 = -8.5\) kcal/mol; \(\Delta S^0 = -11.1\) e.u.; \(-T\Delta S^0 = 3.3\) kcal/mol) reflect this rigidity.\(^8\) The simplicity, conformational rigidity, and ease of modification of vancomycin and DADA, combined with the wealth of relevant structural, thermodynamic, and kinetic information obtained by Perkins, Williams, Griffin, Pratts, and others, make this system an attractive one with which to study the physical-organic chemistry of polyvalent interactions.

Polyvalent binding—the simultaneous interactions of multiple, linked ligands with multiple, linked receptors—is a subject of growing interest in biochemistry.\(^1\)\(^3\) A range of important biological interactions—from the association of IgGs with the surface of a bacterium to the rolling of a leukocyte along the capillary endothelium near a site of inflammation—depend on oligo- or polyvalency.\(^1\)\(^3\) In an ideal case, the contribution of polyvalency to the free energy of binding that would come from linking receptors and ligands would appear primarily in the \(\Delta T\Delta S^0\) term.\(^13\) Thus, for example, the free energy of association of a trivalent receptor—ligand system might be related to that of the monomers by eqs 1–3 (Scheme 2). That is, the enthalpy of the trivalent process would be three times that of the monomer, while the loss in entropy (a term we assume, in the simplest case, to be dominated by translational entropy) would be approximately that of the monomer.

In practice, this formulation of a trivalent association neglects obvious complexities of real molecules. In particular, association might introduce favorable or unfavorable enthalpic terms due to interactions among the linking groups, receptors and ligands, and the modifications of the receptor and ligand required to link them may also modify their association. The entropic term will include contributions from conformational, rotational, and vibrational terms, and from solvent release, in addition to a term due to translational entropy. In trying to understand the interplay of these terms, it seemed to us sensible to study a system in

4 To whom correspondence should be addressed.
5 Department of Chemistry, University of Massachusetts, Amherst, Massachusetts 01003.
which the interacting components were relatively rigid, and in which \( \Delta S^\circ \) was relatively small for the monomers. The system comprising vancomycin and l-Lys-d-Ala-d-Ala met these criteria.

Both vancomycin and DADA can be modified by synthesis,\textsuperscript{14,15} and relatively straightforward procedures can be used to generate polyvalent derivatives of both.\textsuperscript{1} Both the \( \epsilon \)-amino group of the lysine group in l-Lys-d-Ala-d-Ala and the carboxylate group of vancomycin can be modified relatively easily with little influence on the binding constant.\textsuperscript{4,14} Divalency has been inferred to be important in the biological activity of some of vancomycin-type antibiotics.\textsuperscript{16–18} Williams et al. have suggested that spontaneous dimerization (with head-to-tail geometry) of these antibiotics contributes to their tight binding to DADA groups in the bacterial cell wall.\textsuperscript{19} We have examined the interaction of a synthetic dimer of vancomycin (V-CONHCH\( _2 \)C\( _6 \)H\( _4 \)CH\( _2 \)NHCO-V = vancomycin) with a corresponding dimeric derivative of DADA [CH\( _2 \)CONH(N\( ^\epsilon \)-Ac)-l-Lys-d-Ala-d-Ala\( _2 \)], and demonstrated an enhancement in binding of approximately 10\(^3\), relative to unmodified monomeric vancomycin and DADA, and \( N\^3\)-diacetyl-l-Lys-d-Ala-d-Ala.\textsuperscript{1} Here we describe a trivalent system that comprises trimeric derivatives of vancomycin and DADA and that shows remarkably tight binding in water. A preliminary report of this work has appeared.\textsuperscript{2} Understanding the origins of this tight binding—and of the contribution of conformational mobility to it—helps to clarify the nature of oligovalent interactions.

**Results**

**Design and Synthesis of Trivalent Derivatives of Vancomycin, \( R_V^3 \), and of DADA, \( R_L^3 \).** The overall design for these two derivatives was based on the positions available for modification, and on the geometry of the complex (Scheme 1); we use the subscript “\( t \)” to indicate trivalent derivatives. The basic strategy was to use the \( \epsilon \)-amino group of the lysine group of the ligand, and the single carboxylic acid of vancomycin, to form links to central hubs. The design of the central hub for \( R_V^3 \) was critical to the success of our study. It had to be: (i) rigid, to minimize the loss of conformational entropy on binding, and (ii) appropriately reactive, to allow preparation of the desired trivalent derivative of vancomycin. A rigid triamine was designed and synthesized for this purpose (Scheme 3). Coupling of the triamine with vancomycin mediated by 2-(1H-benzotriazol-1-yl)-1,1,3,3-tetramethyluronium hexafluorophosphate (HBTU) was carried out successfully in a mixture of dimethylformamide and dimethyl sulfoxide. Purification of the reaction residue by reverse-phase HPLC afforded the desired product \( R_V^3 \).

The \( R_V^3 \) hexafluoroacetate was isolated as a white foam after lyophilization. The \( ^1H \) NMR spectrum showed the resonances expected for the hub and vancomycin units. The ESI-MS exhibited an ion at \( m/z \) 4818.8; this value is consistent with the average calculated molecular weight of 4817.4 for the parent ion (M + H\(^+\)). Obtaining a pure sample of \( R_V^3 \) was very difficult. We made a substantial effort to purify \( R_V^3 \) and were able to obtain a small amount of \( R_V^3 \) sample that was almost pure (as judged by HPLC analysis; Figure 1A). We used this

![Diagram](Image 423 to 498x721)

**Scheme 1.** Model of Complexes of Vancomycin or Trimeric Vancomycin Derivative \( R_V^3 \) with \( N\^3\)-diacetyl-l-Lys-d-Ala-d-Ala (L) or Trimeric Ligand of DADA \( R_L^3 \). Other details are given in the text.

---


pure sample for calorimetric measurements and for some HPLC experiments. Most of the samples we used in the HPLC studies contained approximately 10% impurities (estimated from the HPLC integration; Figure 1B); these impurities are indicated in the HPLC chromatograms.

A similar strategy was applied to the design of \( \text{R}^\prime \text{L}^\prime_3 \). We used a 1,3,5-benzene tris(carboxamide) as the core so that the structure was compatible in symmetry with \( \text{R}_3 \text{V}_3 \). We synthesized a protected tripeptide precursor, \( \text{N}^{\alpha,L}-\text{diacetyl-}L\text{-Lys-}D\text{-Ala-}D\text{-Ala} \). Coupling of this compound with 1,3,5-benzene tris(carbonyl chloride) afforded protected \( \text{R}^\prime \text{L}^\prime_3 \) (Scheme 3). After deprotection, \( \text{R}^\prime \text{L}^\prime_3 \) was purified by reverse phase HPLC and characterized by \(^1\text{H}\) NMR spectroscopy and ESI-MS.

Association of \( \text{R}_3 \text{V}_3 \) with a Monovalent Ligand. We began the analysis of binding of derivatives of DADA to \( \text{R}_3 \text{V}_3 \) by measuring the binding constant of the vancomycin groups in this species with \( \text{N}^{\alpha,L}-\text{diacetyl-}L\text{-Lys-}D\text{-Ala-}D\text{-Ala} \) (L). In the analysis, we assumed the binding of L to each site of \( \text{R}_3 \text{V}_3 \) to be an independent event with the same affinity (defined by \( K^m_i \); “m” indicates a monovalent association). In the absence of any information to the contrary, the assumption that the binding events are independent is physically reasonable: the three active sites of \( \text{R}_3 \text{V}_3 \) are indistinguishable, they are far apart and separated by a rigid spacer, and there is no obvious mechanism for them to interact with one another (the head-to-tail dimerization observed in monomeric vancomycin \(^{16-18}\) seems to be unlikely, since the three vancomycin units are linked together in a head-to-head fashion). We defined the three stepwise dissociation constants as \( K^m_{d1}, K^m_{d2}, \) and \( K^m_{d3} \), respectively (eqs \( 4-6 \)). After making statistical corrections for the number of binding sites available at each step, the relationships between \( K^m_{d1} \) and the three stepwise dissociation constants are

\( \begin{align*}
1) & \quad 3 \xrightarrow{\text{Monomer}} 3 \\
2) & \quad 3 \xrightarrow{\text{Rigid, Perfectly Fitting Trimer}} 3 \\
3) & \quad 3 \xrightarrow{\text{Flexible Trimer}} 3
\end{align*} \)

\( \Delta G^m_i = 3 \Delta H^m_i - 3 \Delta S^m_i - 3 \Delta S^m_{\text{trans+rot},i} \) (1)

\( \Delta G^m_i = 3 \Delta H^m_i - 3 \Delta S^m_i - 2 \Delta S^m_{\text{trans+rot},i} - \Delta S^m_{\text{conf}} \) (2)

\( \Delta G^m_i = 3 \Delta H^m_i - 3 \Delta S^m_i + 2 \Delta S^m_{\text{trans+rot},i} - \Delta S^m_{\text{conf}} \) (3)

\( (1) \) The total entropic cost of association of three monovalent receptors and three monovalent ligands is \( 3 \Delta S^m_{\text{m}} \). \( (2) \) If the three receptors and three ligands are connected by a perfect rigid linking group (that is, one in which there is neither conformational entropy loss nor enthalpic strain of binding), the entropy loss of binding is approximately \( 3 \Delta S^m_{\text{m}} - 2 \Delta S^m_{\text{trans+rot},m} \) (eq 2; \( \Delta S^m_{\text{conf}} = 0 \)). \( (3) \) Flexible trimers may associate without enthalpic strain but with loss in conformational entropy (eq 3; \( \Delta S^m_{\text{conf}} < 0 \)). If \( \Delta S^m_{\text{conf}} \) is too large, monovalent binding will dominate. \( \Delta G^m, \Delta H^m, \) and \( \Delta S^m \) are the free energy, enthalpy, and entropy of monovalent binding, respectively; \( \Delta S^m_{\text{trans+rot},m} \) is the translational and rotational entropy of monovalent binding. \( \Delta G^m \) is the free energy of trivalent binding, and \( \Delta S^m_{\text{conf}} \) is the loss in conformational entropy in the two intramolecular association events.
defined in these equations. The overall dissociation constant of complex R₃V₃:3L can then be expressed as (K_d)³ (eq 7).

\[
\begin{align*}
R₃V₃·L & \rightleftharpoons R₃V₃·L^\dagger & K_{d1} = (K_d)² \\
R₁V₂·2L & \rightleftharpoons R₁V₂·L + L & K_{d2} = K_d \\
R₃V₃·3L & \rightleftharpoons R₃V₃·2L + L & K_{d3} = 3K_d \\
R₃V₃·3L & \rightleftharpoons R₃V₃ + 3L & K_{d4} = (K_d)³
\end{align*}
\]

Using difference UV spectroscopy, we titrated R₃V₃ with L to estimate K_d. Scatchard analysis yielded the apparent average dissociation constant per binding site, which is, by our definition, K_d. The value of K_d obtained from the plot is approximately 5.0 μM (Figure 2). For comparison, Table 1 gives values of dissociation constants for other relevant compounds; the value of K_d is similar to those measured previously for monomers and dimers. This similarity makes it unlikely that there are large differences between the values for K_m, K_d, and K_d.

Stability of the Complex of R₃V₃·R'L₃. We tested the stability of the complex R₃V₃·R'L₃ under the conditions used for HPLC experiments. We first injected a sample containing R₃V₃ (4.5 μM) into a C₁₈ reverse-phase analytical column and eluted with a linear gradient starting from 85% of solvent A [0.1% trifluoroacetic acid (TFA) in water] and 15% solvent B (0.1% TFA in acetonitrile) to 70% A and 30% B in 45 min (Figure 3A). We observed a peak corresponding to R₃V₃. We then injected a sample containing a 1:1.1 mixture of R₃V₃ and R'L₃ ([R₃V₃] = 4.5 μM and [R'L₃] = 5 μM in 20 mM phosphate buffer at pH 7.0) under the same conditions. On injecting this mixture, we observed only the aggregate R₃V₃·R'L₃ (Figure 3C); we did not observe free R₃V₃ (R₃V₃·R'L₃ and R₃V₃ have clearly distinguishable retention times). The symmetry of the peak did not suggest dissociation or instability. This observation indicates, inter alia, that dissociation of this trivalent aggregate is slow relative to the time required for the HPLC experiment (~45 min).

A control experiment examined a mixture of R₃V₃, and the monomeric ligand L ([R₃V₃] = 4.5 μM; [L] = 19.1 mM in the

![Figure 2](https://example.com/figure2.png)

**Figure 2.** UV difference spectroscopy at 280 nm to determine K_d of L to R₃V₃ at pH 7.0 in the 20 mM phosphate buffer. R₃V₃ (2.1 μM, 3.0 mL) in a 1-cm cell was titrated against a solution of L (8.5 mM). The fraction function r was defined as the ratio of the change in the absorbance at 280 nm to the maximal change (r = ΔA(280)/ΔA(max)).

**Table 1.** Dissociation Constants of Complexes of Vancomycin (V) and Its Derivatives with β-L-Lys-β-Ala-β-Ala-β-Ala

<table>
<thead>
<tr>
<th>vancomycin and derivative</th>
<th>K_d (μM)</th>
<th>ref</th>
</tr>
</thead>
<tbody>
<tr>
<td>V</td>
<td>0.67&lt;sup&gt;a&lt;/sup&gt;</td>
<td>3</td>
</tr>
<tr>
<td>n-C₄H₄-NHCO-V</td>
<td>1.0&lt;sup&gt;b&lt;/sup&gt;</td>
<td>15</td>
</tr>
<tr>
<td>NH₂(CH₂)₃S-S(CH₂)₃NHCO-V</td>
<td>4.3&lt;sup&gt;c&lt;/sup&gt;</td>
<td>20</td>
</tr>
<tr>
<td>V-CO-NH(CH₂)₃S-S(CH₂)₃NHCO-V</td>
<td>3.9&lt;sup&gt;d&lt;/sup&gt;</td>
<td>20</td>
</tr>
<tr>
<td>V-CO-NH(CH₂)₃NHCO-V</td>
<td>1.5&lt;sup&gt;e&lt;/sup&gt;</td>
<td>20</td>
</tr>
<tr>
<td>V-CO-NHCl₃C₄H₇NHCO-V</td>
<td>4.8&lt;sup&gt;f&lt;/sup&gt;</td>
<td>1</td>
</tr>
<tr>
<td>R₃V₃</td>
<td>5.0&lt;sup&gt;g&lt;/sup&gt;</td>
<td>this work</td>
</tr>
</tbody>
</table>

<sup>a</sup> UV difference spectroscopy in 20 mM sodium citrate buffer (pH 5.1). <sup>b</sup> UV difference spectroscopy in 20 mM sodium citrate buffer (pH 5.1). <sup>c</sup> Fluorescence competitive titration in 10 mM HEPES, 6 mM NaCl buffer (pH 7.0).<sup>d</sup> UV difference spectroscopy in 20 mM phosphate buffer (pH 6.9).<sup>e</sup> Estimated error is ±1.5 μM.
same phosphate solution (Figure 3B); that is, a concentration that is approximately 3800 \( K_{d}^{0} \) on HPLC using the same elution conditions; this experiment showed only \( R_{V3} \). We infer that the 1:3 complex of \( R_{V3} \cdot 3 L \) that was undoubtedly present at equilibrium dissociated completely during the passage through the column; the fact that the peak for \( R_{V3} \) was sharp indicates that dissociation was fast under the conditions of the experiment.

We conclude that \( R_{V3} \cdot R'_{L3} \) is stable enough to survive the HPLC experiment intact. We could therefore use HPLC to quantitate the relative quantities of \( R'_{L3} \), \( R_{V3} \), and \( R_{V3} \cdot R'_{L3} \) in a mixture of these species, and to estimate the trivalent dissociation constant.

**Design of the Competitive Binding Assay.** An attempt to determine the trivalent dissociation constant \( K_{d}^{3} \) by a direct titration of \( R_{V3} \) with \( R'_{L3} \) (eq 8) was not successful; the reaction was stoichiometric even when \( R_{V3} \) was at its minimum detectable concentration [in the \( \mu \)M range for the UV detector]. We thus turned to a competition assay to estimate \( K_{d}^{3} \) indirectly from the equilibrium constant \( K \) (eqs 9, 10).

\[
R_{V3} \cdot 3 L + R'_{L3} \stackrel{K}{\rightleftharpoons} R_{V3} \cdot R'_{L3} + 3 L
\]  

(8)

\[
K = \frac{[R_{V3} \cdot R'_{L3}][L]^3}{[R_{V3} \cdot 3 L][R'_{L3}]} = \frac{K_{d}^{3}}{K_{d}^{0}}
\]  

(9)

We allowed \( R'_{L3} \) to compete with the monovalent ligand \( L \) for \( R_{V3} \).

A competition assay is most easily interpreted if the concentration of \( L \) is such that all three of the binding sites of \( R_{V3} \) are fully occupied in the absence of \( R'_{L3} \). The concentration of \( L \) required to saturate 99% of the three vancomycin binding sites, \([L]^{S}_{0}\), is given by eq 11 (see Supporting Information for a detailed derivation). We defined \( \theta \) as a measure of the progress of the displacement reaction as a function of the amount of \( R'_{L3} \) added; \( \theta \) is the fraction of the total \( R_{V3} \) present in the sample that is in the form of \( R_{V3} \cdot R'_{L3} \) (eq 12).

\[
\theta = \frac{[R_{V3} \cdot R'_{L3}]}{[R_{V3} \cdot 3 L] + [R_{V3} \cdot R'_{L3}]}
\]  

(10)

\[
\theta = \frac{[R_{V3} \cdot R'_{L3}]}{[L]^{S}} = \frac{K_{d}^{3}}{K_{d}^{0}} \theta + \frac{K_{d}^{3}}{[L]^{S}_{0}}
\]  

(13)

The competition assay depends on being able to establish three concentrations: \([R_{V3} \cdot R'_{L3}], [R'_{L3}], \) and \([R_{V3} \cdot 3 L] \) in a solution containing \( L \) at a fixed concentration \([L]^{0}_{0} \), and \( R'_{L3} \) at a variable concentration. Under the conditions used in these experiments, the complex \( R_{V3} \cdot 3 L \) dissociates rapidly; the only peak observed in HPLC on injection of this complex is uncomplexed \( R_{V3} \). The stability of the complex \( R_{V3} \cdot R'_{L3} \), and the ability to separate these species on HPLC, allowed us to use an HPLC assay to establish their relevant concentrations at equilibrium in the solution. We established \( [R_{V3} \cdot 3 L] \) indirectly by measuring the concentration of one of the species, \( R_{V3} \), derived from it by dissociation. On the basis of the HPLC experiments described previously, we assume that \( R_{V3} \cdot 3 L \) (and any traces of \( R_{V3} \cdot 2 L \) and \( R_{V3} \cdot L \) present) are converted quantitatively to \( R_{V3} \) on the HPLC column by rapid dissociation of \( L \).

**Analysis of the Competitive Binding Assay and Estimation of \( K_{d}^{3} \).** For \( K_{d}^{0} \approx 5.0 \, \mu M \), a concentration of \( L \) of \( \sim 1.5 \, mM \) in solution ensures that 99% of the binding sites of \( R_{V3} \) are occupied by \( L \) (eq 11). We used a value of \([L]^{S}_{0} \approx 19.1 \, mM (\geq 10 \text{ times larger than 1.5 mM}); because the binding of \( R'_{L3} \) to \( R_{V3} \) was so tight, a high value of \([L] \) was required to give a quantifiable concentration of \( R'_{L3} \) in solution at equilibrium in the system used in the competition experiments (described by eq 9). Aliquots of a stock solution of \( R'_{L3} \) (1.06 mM) were added to a solution of \( R_{V3} \) (4.5 \, \mu M) and \( L \) (19.1 mM) in 20 mM pH 7.0 phosphate buffer. After each addition of \( R'_{L3} \), the solution was mixed by vortexing and allowed to equilibrate for about 40 min at room temperature (about 30 °C). A sample was removed and examined by HPLC, eluting with a linear gradient from 85% solvent A (0.1% TFA in water) and 15% solvent B (0.1% TFA in acetonitrile) to 70% A and 30% B over 45 min. Under these conditions, \( R_{V3} \cdot 3 L \) dissociated into its components on injection and appeared as separate peaks for \( R_{V3} \) and \( L \). \( R_{V3} \cdot R'_{L3} \) was stable and appeared as a well-defined peak. Additional aliquots of \( R'_{L3} \) were added until free \( R_{V3} \) could no longer be detected by HPLC. Figure 4 shows the HPLC chromatograms of a representative titration.

Since \( L \) is present in large excess relative to \( R_{V3} \), we assume that the concentration of \( L \), at equilibrium, is the same as its initial concentration, [\( L \) \] \( \approx [L]^{0}_{0} \). Analysis of the data requires a relationship between \( \theta \) (eq 12) and \([R'_{L3}] \). Equation 13,

\[
\theta = \frac{[R_{V3} \cdot R'_{L3}]}{[L]^{S}} = \frac{K_{d}^{3}}{K_{d}^{0}} \theta + \frac{K_{d}^{3}}{[L]^{S}_{0}}
\]  

(13)

obtained by combination of eqs 10 and 12, was used to characterize the binding: if the ratios of \( \theta/[R'_{L3}] \) are plotted versus \( \theta \), a straight line would be expected; both the slope and


(22) Our analyses assume that the two intermediate species, \( R'_{L3} \cdot R_{V3} \cdot 2 L \) and \( R'_{L3} \cdot R_{V3} \cdot L \), are present in very small amounts at equilibrium and can thus be neglected. This assumption leads to eq 13, which predicts a linear plot of \( \theta/[R'_{L3}] \) versus \( \theta \). The agreement of our experimental results with this prediction suggests that this assumption is valid under our experimental conditions.

(23) The value of the rate constant for dissociation of the monovalent complex of vancomycin with \( L \) is \( k_{d} = 31 \, s^{-1} \) (ref 21).
Design of a High-Affinity Trivalent System

Figure 4. HPLC chromatograms of the titrated solution of R\textsubscript{V3} (4.5 μM) on addition of aliquots of R′L\textsubscript{3}′ (1.06 mM) solution in the presence of L (19.1 mM). The sample of R\textsubscript{V3} used here contained small amounts of impurities, which are indicated by the symbols (*). The HPLC conditions were similar to those described in Figure 3, except that a Vydac analytical RP column was used with the same linear gradient, run over 30 min.

y-intercept of this line would afford the ratio of $K/|L|^3$ and thus the value of $K$. The values of $|R′L′_3|$ were estimated from integration of the peaks for R′L′\textsubscript{3} on the HPLC; $\theta$ was calculated (eq 12) using the integrated intensities of R\textsubscript{V3}R′L′\textsubscript{3} and R\textsubscript{V3}. The Experimental Section details the procedure. The fact that the sum of the two integrals of the peaks of R\textsubscript{V3}, R′L′\textsubscript{3} and R\textsubscript{V3} during the titration was approximately constant indicates that no species other than those in eq 9 were present in significant amounts at equilibrium. The ratios of $\theta/|R′L′_3|$ were then plotted versus $\theta$. As expected, the plot gave a straight line and yielded the value of $K$ (Figure 5). We estimated $K_d$ using $K_{dm}$ and $K$ (eq 10); our estimate of $K_d$ is $\sim 4 \pm 1 \times 10^{-17}$ M.

Exchange Reaction Between R\textsubscript{V3}, R′L′\textsubscript{3} and L. At first, the conclusion that R\textsubscript{V3} bound very tightly to R′L′\textsubscript{3} seemed at odds with the relatively fast equilibration we observed in solutions containing R\textsubscript{V3}, R′L′\textsubscript{3}, and L. We therefore turned to an examination of the rates of equilibrium of the species involved in this system. If we assume that $k_{on}$ for association of R\textsubscript{V3} and R′L′\textsubscript{3} is 9 times that for association of V and L\textsuperscript{21} (making a statistical correction of a factor of 9 for the number of receptor and ligand groups in the trimeric species), then $k_{on}$ would be $\sim 2.5 \times 10^9$ M$^{-1}$ s$^{-1}$, and $k_{off}$ for R\textsubscript{V3}R′L′\textsubscript{3} = $k_{on}$ $K_d$ $\approx 1 \times 10^{-8}$ s$^{-1}$. Even if we assume that the rate for association of R\textsubscript{V3} with R′L′\textsubscript{3} is diffusion controlled (which may be true for antibodies and certain other proteins but is probably not true for association of R\textsubscript{V3} and R′L′\textsubscript{3} by extension from the kinetic behavior of the monomeric species), and has a value of $k_{on} \approx 10^9$ M$^{-1}$ s$^{-1}$, the value of $k_{off}$ would be $\sim 4 \times 10^{-8}$ s$^{-1}$. This value implies that dissociation of R\textsubscript{V3}R′L′\textsubscript{3} would be too slow to be observed directly. This implication is consistent with our observation that the aggregate is stable for $>10^3$ s under HPLC conditions.

The exchange reaction between R\textsubscript{V3}, R′L′\textsubscript{3} and L proceeded surprisingly rapidly, however (equilibration was complete in
used to monitor the progress of the exchange reaction; dansyl-

Thermodynamic Parameters of Binding of Derivatives of Vancomycin to Derivatives of DADA at 298 K

Table 2. Thermodynamic Parameters of Binding of Derivatives of Vancomycin to Derivatives of DADA at 298 K

<table>
<thead>
<tr>
<th>receptor</th>
<th>ligand</th>
<th>receptor/ligand</th>
<th>valency</th>
<th>$K_d$ (M)</th>
<th>$\Delta G^\circ$ (kcal/mol)</th>
<th>$\Delta H^\circ$ (kcal/mol)</th>
<th>$-T\Delta S^\circ$ (kcal/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R V_3$</td>
<td>$R L_3'$</td>
<td>1:1</td>
<td>tri</td>
<td>$4 \times 10^{-17}$</td>
<td>$-22$</td>
<td>$(-7.3)$</td>
<td>$(-13.3)$</td>
</tr>
<tr>
<td>$V$</td>
<td>$L$</td>
<td>1:1</td>
<td>mono</td>
<td>$1.6 \times 10^{-6}$</td>
<td>$-7.9$</td>
<td>$-12.0$</td>
<td>4.1</td>
</tr>
<tr>
<td>$R V_3$</td>
<td>$R L_3'$</td>
<td>1:3</td>
<td>mono</td>
<td>$1.1 \times 10^{-6}$</td>
<td>$-8.1$</td>
<td>$-12.4$</td>
<td>4.3</td>
</tr>
<tr>
<td>$R V$</td>
<td>$R L_3'$</td>
<td>1:3</td>
<td>mono</td>
<td>$2.7 \times 10^{-6}$</td>
<td>$-7.6$</td>
<td>$-12.0$</td>
<td>4.4</td>
</tr>
<tr>
<td>$V$</td>
<td>$L$</td>
<td>3:1</td>
<td>mono</td>
<td>$0.34 \times 10^{-6}$</td>
<td>$-8.8$</td>
<td>$-17.5$</td>
<td>8.7</td>
</tr>
<tr>
<td>$R V$</td>
<td>$R L_3'$</td>
<td>3:1</td>
<td>mono</td>
<td>$0.11 \times 10^{-6}$</td>
<td>$-9.5$</td>
<td>$-17.8$</td>
<td>8.3</td>
</tr>
<tr>
<td>$R V$</td>
<td>$R L_3'$</td>
<td>1:1</td>
<td>mono</td>
<td>$0.96 \times 10^{-6}$</td>
<td>$-8.2$</td>
<td>$-21.0$</td>
<td>13</td>
</tr>
</tbody>
</table>

Values of $\Delta H^\circ$ were determined by ITC titrations at pH 7.0 in 5.0 mM phosphate buffer at 298 K. Values of $\Delta G^\circ$ were determined from $K_d$ measured in the same solution, except for that of $R V_3$; $R L_3'$. Values of $-T\Delta S^\circ$ were calculated from $\Delta G^\circ = \Delta H^\circ - T\Delta S^\circ$. Each titration was at least duplicated and differences are within 25% for $K_d$ and 5% for $\Delta H^\circ$. All thermodynamic values refer to the monovalent interaction between individual units of $V$ and individual units of $L$ or $L'$, except for those for binding of $R V_3$ to $R L_3'$. For convenience, the average values per $V$-$L$ binding are also given for $R V_3$-$R L_3'$, and indicating by the label “mono” and brackets $\langle \rangle$. $\d$ Measured in 20 mM phosphate buffer at 25 °C by ITC; our values agree well with the literature values. 26 $\d$ In the cases of 1:3 or 3:1 binding, the values of $K_d$ are $K_d^\d$, the average dissociation constant per site (defined by eqs 4–7); these values are statistically corrected for the presence of multiple binding sites. Refer to Scheme 1 for structures of $R V_3$ and $R L_3'$, and Scheme 4 for structures of $R V$ and $R L'$.

Figure 7. ITC titration of $R V_3$ by $R L_3'$ (0.126 mM) in 5.0 mM phosphate buffer at 298 K. The injected volumes of the first, second, and twelfth injections were 0.5, 3.5, and 35 µL, respectively, and the remaining injections. The interval between the second and third injections was 20 min; the interval between the remaining injections was 5 min.

Table 2. Thermodynamic Parameters of Binding of Derivatives of Vancomycin to Derivatives of DADA at 298 K

<table>
<thead>
<tr>
<th>receptor</th>
<th>ligand</th>
<th>receptor/ligand</th>
<th>valency</th>
<th>$K_d$ (M)</th>
<th>$\Delta G^\circ$ (kcal/mol)</th>
<th>$\Delta H^\circ$ (kcal/mol)</th>
<th>$-T\Delta S^\circ$ (kcal/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R V_3$</td>
<td>$R L_3'$</td>
<td>1:1</td>
<td>tri</td>
<td>$4 \times 10^{-17}$</td>
<td>$-22$</td>
<td>$(-7.3)$</td>
<td>$(-13.3)$</td>
</tr>
<tr>
<td>$V$</td>
<td>$L$</td>
<td>1:1</td>
<td>mono</td>
<td>$1.6 \times 10^{-6}$</td>
<td>$-7.9$</td>
<td>$-12.0$</td>
<td>4.1</td>
</tr>
<tr>
<td>$R V_3$</td>
<td>$R L_3'$</td>
<td>1:3</td>
<td>mono</td>
<td>$1.1 \times 10^{-6}$</td>
<td>$-8.1$</td>
<td>$-12.4$</td>
<td>4.3</td>
</tr>
<tr>
<td>$R V$</td>
<td>$R L_3'$</td>
<td>1:3</td>
<td>mono</td>
<td>$2.7 \times 10^{-6}$</td>
<td>$-7.6$</td>
<td>$-12.0$</td>
<td>4.4</td>
</tr>
<tr>
<td>$V$</td>
<td>$L$</td>
<td>3:1</td>
<td>mono</td>
<td>$0.34 \times 10^{-6}$</td>
<td>$-8.8$</td>
<td>$-17.5$</td>
<td>8.7</td>
</tr>
<tr>
<td>$R V$</td>
<td>$R L_3'$</td>
<td>3:1</td>
<td>mono</td>
<td>$0.11 \times 10^{-6}$</td>
<td>$-9.5$</td>
<td>$-17.8$</td>
<td>8.3</td>
</tr>
<tr>
<td>$R V$</td>
<td>$R L_3'$</td>
<td>1:1</td>
<td>mono</td>
<td>$0.96 \times 10^{-6}$</td>
<td>$-8.2$</td>
<td>$-21.0$</td>
<td>13</td>
</tr>
</tbody>
</table>

<45 min), as shown by HPLC during the exchange of $R V_3$; $R L_3'$ with excess $L$ (Figure 6). We prepared the initial solution of $R V_3$-$R L_3'$ by mixing 3 µM of $R V_3$ and 22 µM of $R L_3'$ in 20 mM phosphate solution. Examination of the sample by HPLC (using conditions similar to those used in the competition experiments) established that $R V_3$-$R L_3'$ had formed (Figure 6). Then $L$ was added to this solution of $R V_3$-$R L_3'$ in quantities sufficient to make the concentration of $L$ about 86 mM. At intervals, samples were withdrawn and examined by HPLC. Exchange of $R V_3$-$R L_3'$ with $L$ yielded the complex of $R V_3$-$3L$: this complex dissociated on the HPLC column to free $R V_3$ (as discussed previously). The integrated areas of the peaks for $R V_3$-$R L_3'$ and $R V_3$ (derived by dissociation of $R V_3$-$3L$) were used to monitor the progress of the exchange reaction; dansyl-L-Leu was again used as an internal standard. Equilibration was complete within 45 min, and no further significant change in peak intensities occurred after that time. Approximately 60% of the $R V_3$ remained as $R V_3$-$R L_3'$ at equilibrium in a system containing $L$ at a concentration of $\sim$86 mM; this value of $L$ is $\sim$17 000 times greater than that of the dissociation constant for the complex of $R V_3$ and $L$, and confirmed that $R V_3$-$R L_3'$ was tightly associated.

Scheme 4. Structures of the Monovalent Derivatives of DADA and $V$, $R L_3'$, and $R V$, Respectively

There is an essential difference in kinetics between this trivalent system and biotin-avidin. Dissociation of biotin-avidin necessarily proceeds to completion in one step and is slow.24

The presence of a large excess of biotin does not accelerate the dissociation of biotin-avidin. As we have demonstrated here, dissociation of R_t V_3 to R_t L_3 is slow in isolation, but rapid when carried out in the presence of excess monovalent ligand L. Dissociation of R_t V_3 to R_t L_3 therefore proceeds by a mechanism different from that of the single-step dissociation of biotin-avidin. We discuss the kinetics of this dissociation in the Discussion section.

Estimation of $\Delta H^o$ of the Binding of R_t V_3 to R_t' L_3. A direct estimation of $\Delta H^o$ for the association of R_t V_3 with R_t' L_3 would separate $\Delta G^o$ into enthalpic and entropic terms, and clarify the thermodynamic basis for the very high binding constant of this receptor/ligand pair. We have characterized the association of R_t V_3 with R_t' L_3 using isothermal titration calorimetry (ITC). ITC can be used to estimate dissociation constants ($K_d$) in the millimolar to nanomolar range. It allowed us to estimate both the enthalpy of binding, $\Delta H^o$, and the dissociation constant $K_d^m$ for the monovalent interactions, but only $\Delta H^o$ for the interaction of R_t V_3 with R_t' L_3. Experiments were carried out by adding aliquots of a solution of R_t V_3 (~0.126 mM) in 5.0 mM phosphate buffer to a solution of R_t V_3 (~3 $\mu$M) in 5.0 mM phosphate buffer in the cell of the calorimeter (Figure 7). By integration of the peaks, we estimated $\Delta H^o$ to be $-40$ kcal/mol (Table 2). Titrations were repeated three times and the maximum difference among these values of $\Delta H^o$ was less than 2 kcal/mol. The value of $T \Delta S^o$ for binding of R_t V_3 to R_t' L_3 is thus approximately $-18$ kcal/mol ($T \Delta S^o = \Delta H^o - \Delta G^o$). The value of $\Delta H^o$ for the binding of vancomycin to L has been reported as $-12.8$ kcal/mol. The value of $\Delta H^o$ of the trivalent system is thus approximately three times that for monovalent vancomycin and DADA, and the value of $T \Delta S^o$ for the trivalent system is approximately 4.5 times that for the monovalent system.

We were also concerned about the effect of the interaction between the two linking groups in R_t V_3 and R_t' L_3 on the binding in the trivalent system. We therefore synthesized two monovalent derivatives of DADA and V, R_t' L' (N$^\alpha$-acetyl-N$^\alpha$-benzoyl-1-Lys-d-Ala-d-Ala) and RV (C_6H_4CONHC_6H_4-4-CH_2NHCOV), respectively (Scheme 4), to simulate the influence of the R_t group in R_t V_3 and the R_t group in R_t V_3. The ITC titrations characterized the interactions between these ligand/receptor pairs thermodynamically, and Table 2 summarizes the results.

All of the bindings examined in Table 2 are monovalent except that for the binding of R_t V_3 to R_t' L_3. The parameters listed in this table thus referred to monovalent binding between V (or V unit in R_t V_3) and its ligand except in the binding of R_t V_3 to R_t' L_3. In particular, in the cases of 1:3 or 3:1 complexes, the dissociation constant ($K_d$) refers to a monovalent dissociation constant ($K_d^m$ with units of molar), not a collective constant (a product of three monovalent binding constants, which is equal to ($K_d^m$)^3) and which has units of M$^{-3}$; eqs 4–7). The results indicate that the value of $K_d$ is essentially indifferent to substitution on either vancomycin or L-Lys-d-Ala-d-Ala groups, so long as the interaction is monovalent; only the trivalent interaction is exceptionally strong. In broad terms, the data suggest that the high free energy of association of R_t V_3 · R_t' L_3 originates primarily in the enthalpy of association of three V and L groups. The values of $\Delta H^o$ of binding of V, or of its monomeric derivative RV to R_t' L_3 are, however, about 5 kcal/mol more negative than that of V to L. A discussion of these thermodynamic data follows in the next section.

Discussion

The dissociation constant describing the dissociation of R_t V_3 · R_t' L_3 into R_t V_3 + R_t' L_3 ($K_d \approx 4 \times 10^{-17}$ M) is $10^{-10}$ that of

---

V-L into V + L ($K_a^0 \approx 1.6 \times 10^{-6} \text{ M})^2$. The relationship between thermodynamic and kinetic characteristics of this dissociation is strikingly different from that of avidin-biotin: although the rate of dissociation of R$_V$3.L3 is slow (as is that of avidin-biotin), equilibration of R$_V$3.L3 with monomeric L to give R$_V$3.L3 is relatively fast, and monomeric L competes relatively effectively with trimeric R$_V$3.L3 for the receptor sites on R$_V$3. We consider the issues of kinetics and thermodynamics separately.

**Kinetics.** The essential difference between R$_V$3.L3 and biotin-avidin is that dissociation of the former, when carried out in the presence of excess L, proceeds in three steps, while the latter necessarily proceeds to completion in one step. We considered two plausible mechanisms for the exchange reaction between R$_V$3.L3 and excess L.

**A. Mechanism I.** The first mechanism (Scheme 5) involves complete dissociation of R$_V$3.R′.L3 into R$_V$3 and R′.L3, followed by association of free R$_V$3 with three equivalents of L. This mechanism is similar to that for dissociation of biotin-avidin, which proceeds to completion in one step. We presume that the rate-determining step in this mechanism would be the last one: that is, the step leading to complete dissociation of R$_V$3.R′.L3 into R$_V$3 + R′.L3. The rate of this process would be independent of [L], and would, as we have indicated, be very slow ($k_{diss} \approx 10^{-8} \text{ s}^{-1}$, even if $k_{on}$ were diffusion limited). This expectation is contrary to the experimental observation that, in the presence of excess L, exchange of R$_V$3.L3 with L is complete within 45 min. We therefore discard this mechanism.

**B. Mechanism II.** The second mechanism (Scheme 6) involves a sequence of successive dissociation and association events occurring at the vancomycin binding sites of R$_V$3.L3. After initial dissociation of DADA groups (A → B; C → D), the empty binding sites could associate with L (B → C; D → E) before the next step of dissociation. Association of L with each empty active site would inhibit rebinding of dissociated DADA groups on R′.L3. This mechanism predicts a fast exchange between R$_V$3.R′.L3 and L and is consistent with our experimental observations. We therefore infer that excess monovalent ligand L competes for the binding sites of R$_V$3 on a site-by-site basis and thus accelerates the dissociation of the trivalent complex of R$_V$3.R′.L3.

**C. Kinetics of Association of R$_V$3 with R′.L3.** Scheme 7 outlines the stepwise association of R$_V$3 with R′.L3. So far, we have not been able to measure the rate constants for each kinetic step in this model experimentally. We thus applied rate constants obtained for the monovalent interaction between V and L to an estimate of theoretical values of the kinetic parameters in the binding of R$_V$3 to R′.L3. This estimate should also provide insight into the kinetic origin of the high stability of R$_V$3.R′.L3. We make three assumptions in our estimation. (i) The value of the rate constant for the first step in association of R$_V$3 with R′.L3, $k_1$, is 9 times that of $k_{on}$ for monomeric V and L: $k_1 = 9 k_{on}$. (ii) The rate constant for dissociation of each V/DADA pair in R$_V$3.R′.L3 is, after corrections for statistical factors, approximately the same as $k_{off}$ for V.L, $k_i = k_i/2 = k_i/3 = k_{off}$. (iii) The rate constants of the two intramolecular associations, after corrections for statistical factors, are approximately the same: $k_2/4 = k_3$. Combining these assumptions and the literature values of $k_{off}$ and $k_{on}$ for V and L, ($k_{on} \approx 2.8 \times 10^7 \text{ M}^{-1} \text{ s}^{-1}$; $k_{off} \approx 30 \text{ s}^{-1}$), we estimated $k_2$ and $k_3$ as follows

$$K_d = (k_{-1}k_{-3})(k_2k_3)$$

$$= (30 \times 2 \times 30 \times 30)/(9 \times 2.8 \times 10^7 k_2k_3)$$

$$\approx 4 \times 10^{-17} \text{ M}$$

(14)

With the assumption that $k_2/4 = k_3$, we estimated the rate...
constants for the intramolecular association to be $k_2 = 8 \times 10^6$ s$^{-1}$ and $k_3 = 2 \times 10^6$ s$^{-1}$. These large values of the rate constant for intramolecular association inside the complex suggest the kinetic origin of the high stability of $R_V R'_L ^3$: fast intramolecular rebinding of partially dissociated $V/DADA$ pairs in the complex. (This estimation is obviously highly approximate; it does not consider possible variations in the off-rate in each step of dissociation).

For a value of $k_2 = 8 \times 10^6$ s$^{-1}$, the value of effective molarity of the DADA group is approximately 290 mM ($k_2/k_3 = 8 \times 10^6$ s$^{-1}/2.8 \times 10^7$ M$^{-1}$ s$^{-1}$), and a value of $k_3 = 2 \times 10^6$ s$^{-1}$ corresponds to an effective molarity of about 70 mM. For comparison, Table 3 lists values of effective molarity for several intramolecular processes.\(^{27-33}\) The values of effective molarity in our system, in general, are comparable to (slightly larger than) those for most biochemical systems, but they are smaller than those observed in systems involving smaller components (for example, the chelate effect in the coordination of small ligands with metal ions). This fact indicates that intramolecular binding in our system does not convey as much advantage as it does in chelation of metal ions. Our analysis of the entropic loss in this trivalent system suggests that the relatively small value of effective molarity that we observe here is due to loss in conformational entropy.

One interesting inference from this analysis is that exceptionally high values of effective molarity are not necessarily required to achieve very tight binding in the system $R_V R'_L ^3$. We would, thus, anticipate that a number of systems of receptors and ligands might give very tight binding in tri- or higher-valent form.

**Thermodynamics.** The free energy of trivalent binding of $R_V R'_L ^3$ is approximately three times that of monovalent binding of $V$ to $L$ (Table 2): that is, $\Delta G^\circ_a \approx 3 \Delta G^\circ_m \approx 3 \Delta H^\circ_m$.

<table>
<thead>
<tr>
<th>Receptor</th>
<th>Ligand</th>
<th>Effective molarity $^a$ (M)</th>
<th>ref</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R_V R'_L ^3$</td>
<td>$R'_L ^3$</td>
<td>0.07; 0.29</td>
<td>This study</td>
</tr>
<tr>
<td>Dimeric $V$</td>
<td>Dimeric DADA</td>
<td>0.02</td>
<td>1</td>
</tr>
<tr>
<td>Dimeric $V$</td>
<td>AcKDADA</td>
<td>0.04 $^b$</td>
<td>28</td>
</tr>
<tr>
<td>Non-covalent dimer of Ristocetin A</td>
<td>$N$-decanoyl-DADA</td>
<td>0.01 $^c$</td>
<td>29</td>
</tr>
<tr>
<td>Mammalian hepatic lectin for Galactose (Gai)</td>
<td>$\mu$Gal$^4$-$\mu$GlcNAc$^4$</td>
<td>0.03</td>
<td>30</td>
</tr>
<tr>
<td>Mammalian hepatic lectin for Galactose (Gai)</td>
<td>$\mu$Gal$^4$-$\mu$GlcNAc$^2$</td>
<td>0.03</td>
<td>30</td>
</tr>
<tr>
<td>Mammalian hepatic lectin for Galactose (Gai)</td>
<td>$\mu$Gal$^4$-$\mu$GlcNAc$^2$</td>
<td>0.03</td>
<td>30</td>
</tr>
<tr>
<td>Rabbit $\gamma$-anti-DNP antibody $^f$</td>
<td>bacteriophage conjugated with DNP</td>
<td>0.04</td>
<td>31</td>
</tr>
<tr>
<td>$\beta$-CD $^-S_3$ $\beta$-CD $^f$</td>
<td>cholesterol</td>
<td>0.02</td>
<td>32</td>
</tr>
<tr>
<td>$\beta$-CD $^-S_3$ $\beta$-CD</td>
<td>-</td>
<td>0.01</td>
<td>32, 33</td>
</tr>
<tr>
<td>$\beta$-CD $^-S_3$ $\beta$-CD</td>
<td>-</td>
<td>0.02</td>
<td>33</td>
</tr>
<tr>
<td>EDTA $^f$</td>
<td>Cu$^{2+}$</td>
<td>126</td>
<td>34</td>
</tr>
<tr>
<td>*</td>
<td>Zn$^{2+}$</td>
<td>$8.7 \times 10^3$</td>
<td>34</td>
</tr>
<tr>
<td>*</td>
<td>Cd$^{2+}$</td>
<td>$7.8 \times 10^2$</td>
<td>34</td>
</tr>
</tbody>
</table>

$^a$ Calculated from the reported values of $K_a$. $^b$ Presented at a self-assembly monolayer on gold. $^c$ In the presence of sodium dodecysulfate. $^d$ Assuming that the values of effective molarity for the two intramolecular associations are the same in this trivalent binding. $^e$ DNP: 2,4-dinitrophenyl group. $^f$ $\beta$-CD: $\beta$-cyclodextrin. $^g$ EDTA: ethylenediaminetetraacetate.

$-3T\Delta S^\circ_m$. Calorimetric measurements indicated that $\Delta H^\circ$ for association of $R_V R'_L ^3$ and $R'_L ^3$ ($\sim 40$ kcal/mol) is approximately three times that for $V$ and $L$ ($\Delta H^\circ = -12.8$ kcal/mol). The value of $-T\Delta S^\circ$ for association of the two trivalent species is thus 18 kcal/mol; this value is approximately 4.5 times that of $V$ and $L$ ($T\Delta S^\circ = -4.1$ kcal/mol) (Table 2). In the simplest analysis, we envision two limiting cases for association of $R_V R'_L ^3 + R'_L ^3$ (Scheme 2). In one, after the first $V$ and $L'$ group interact, the other two pairs of $V$ and $L'$ groups are correctly
positioned to interact with negligible further loss in entropy; in this case, \( \Delta G^\circ \approx 3 \Delta H^m_\text{m} - T \Delta S^m_\text{m} + 2T\Delta S^\text{trans-rot,m} \) (\( T\Delta S^\text{trans-rot,m} \) is the translational and rotational entropy for the association of \( V \) and \( L \)). In the second, the linkers are so long and flexible that after interaction of the first \( V \) and \( L \) pair, there is large entropic penalty (conformational entropy loss) that prevents any further intramolecular association. In practice, interactions involving the linkers and hubs can make \( \Delta H^\circ \), different from \( 3 \Delta H^m_\text{m} \), and can also disguise any simple relationship between \( T\Delta S^m_\text{m} \), and \( T\Delta S^\circ \).

We wish to understand the thermodynamic origins of these values. This task would require separating the enthalpic and entropic contributions of each binding event to the free energy of the association of the two trivalent species. Unfortunately, we do not have the information required to carry out this separation, and given the fact that we do not observe intermediates in association or dissociation in HPLC analyses, we are unlikely to be able to obtain this information. Instead, we have inferred the enthalpic and entropic contributions of certain binding events to the \( \Delta G^\circ \) of trivalent binding from semiquantitative analyses of \( \Delta H^\circ \) and \( T\Delta S^\circ \).

\( \Delta H^\circ \). To analyze the value of \( \Delta H^\circ \), we need first to decide on the appropriate reference value to which \( \Delta H^\circ \) should be compared: that is, should the reference value for the "comparable" monomeric interaction, \( \Delta H^m_\text{m} \), be considered the value for \( V \) and \( L \) or for these species with linkers attached? And if the latter, what types of linkers? Our instinct is that the most appropriate structural comparisons for processes involving \( R_t V_3 \) and \( R_t L_3 \) will be derivatives of \( V \) and \( L \) that have linking groups attached, but it is difficult to justify this instinct analytically: unfortunately, we cannot draw a clear conclusion concerning the influence of structures that are, or mimic, the linking groups on the values of \( \Delta H^m_\text{m} \). Table 2 contains values of enthalpy that range from that for \( V + L \) (\( \Delta H^m_\text{m} \approx -12 \text{ kcal/mol} \) or \( 9 \text{ kcal/mol} \), or \( 17.5 \text{ kcal/mol} \) for reference monomers.

We have considered three explanations for the differences in \( \Delta H^\circ \) for the compounds in Table 2: (i) experimental error, (ii) linker–vancomycin interactions, and (iii) dimerization of vancomycin. We discuss each in turn.

**Experimental Error.** A troublesome aspect of the data in Table 2 is the observation that, with the exception of \( R_t V_3 + R_t L_3 \), \( \Delta G^\circ \) varies by less than 1.5 kcal/mol, while \( \Delta H^\circ \) (and of course \( T\Delta S^\circ \)) varies by 9 kcal/mol. The appearance of apparent example of enthalpy/entropy compensation is always a warning, although Williams and others have made a convincing case for the existence of compensating relationships in circumstances in which tighter binding (and a more negative enthalpy of binding) is accompanied with loss in conformational mobility (and a greater loss in entropy). In the data in Table 2, the historically most common and plausible origin of an artifactual enthalpy/entropy compensation—an inaccurate decomposition of \( \Delta G^\circ \) into \( \Delta H^\circ \) and \( T\Delta S^\circ \) based on the temperature dependence of \( \Delta G^\circ \)—is eliminated since \( \Delta G^\circ \) and \( \Delta H^\circ \) were obtained using independent experimental techniques (UV or HPLC for \( \Delta G^\circ \); ITC for \( \Delta H^\circ \)). The values were also consistent over three replications. We therefore believe that they are accurate within the stated uncertainties, and that, as usual, the trends are even more reliable than the numerical data.

Having said that we are confident that the data are largely free of artifact, we point out that they are not simple: we do not see an obvious, qualitative explanation for the trends. For example, for most of the data, increasing the molecular surface of the molecule containing the DADA group increases \( \Delta H^\circ \), but the value for \( R_t V_3 + R_t L_3 \) is an exception. We therefore believe, but cannot prove, that increases in contacting surface and changes in entropy, probably due to restrictions on conformational mobility, compensate.

**Linker–Vancomycin Interactions.** We examined possible contributions of the linker groups to the enthalpy of binding. The values of \( \Delta H^\circ \) for binding of \( R_t V_3 \) to monovalent ligands \( (L \text{ or } R_t L_3') \) are similar to that for the binding of \( V \) to \( L \). This result, by itself, seems to imply that the contribution of the linker groups to \( \Delta H^\circ \) is small. The value of \( \Delta H^\circ \) for binding of \( R_t L_3' \) to \( RV \) (a monovalent vancomycin containing an R group that was designed to simulate the structure of \( R_t \)) is, however, about 5 kcal/mol more negative than that for \( V \) to \( L \) (Table 2). This result seems to conflict with the previous implication that the influence of the linker groups on the value of \( \Delta H^\circ \) is small. Moreover, the value of \( \Delta H^\circ \) for binding of \( R_t L_3' \) to \( V \) was, surprisingly, still approximately 5 kcal/mol more negative than that for binding of \( V \) to \( L \), although only \( R_t L_3' \) bears a linker group in this binding pair. We do not see a simple, consistent relationship between linker groups and their contributions to binding enthalpies that makes it clear what the appropriate reference compound is against which to compare the thermodynamic values for binding of \( R_t V_3 \) to \( R_t L_3' \).

**Dimerization of Vancomycin.** Vancomycin has a strong tendency to form a noncovalent dimer. 16–18 This tendency to dimerize is enhanced by ligand binding. 34 The pattern of dimerization identified by Williams is head-to-tail, and this geometry is not possible for the vancomycin groups of \( R_t V_3 \). It is more plausible that it might play a role for the combination of \( V \) (or \( RV \)) interacting with \( R_t L_3' \), but we have, at present, no direct evidence for or against dimerization of vancomycin as a process that influences the thermodynamics of this system.

**\( T\Delta S^\circ \).** There is an approximately 18 kcal/mol loss of entropy on association of \( R_t V_3 \) with \( R_t L_3' \). As we discussed previously (Scheme 7), the trivalent binding process takes place in three steps: a bimolecular association as the first binding event, then two intramolecular binding steps. The problem in any analysis of \( T\Delta S^\circ \) for the trimeric interaction is, however, the same as that mentioned for \( \Delta H^\circ \): that is, deciding on an appropriate reference value of \( T\Delta S^\circ \).

We have analyzed the value of \( T\Delta S^\circ \) for association of \( R_t V_3 + R_t L_3' \) assuming, for explicitness, that the association of \( V \) to \( L \) provides an appropriate reference value. For the first binding event, we assume that the loss in entropy is mainly associated with translational and rotational terms. The effect of molecular size on the loss of translational and rotational entropy is relatively small (15% for an increase in molecular weight of a factor of 3). For binding of \( V \) to \( L \), \( T\Delta S^\circ \) is \( \approx -4.1 \text{ kcal/mol} \). We thus assume the value of \( T\Delta S^\circ \) for the first binding step of association of \( R_t V_3 + R_t L_3' \) to be \( \approx -4.7 \text{ kcal/mol} \) (based on this 15% correction). We expected the next two steps to be less entropically unfavorable than the first, since they take place intramolecularly. The total value of \( T\Delta S^\circ \) for these two steps is, however, a surprisingly negative number: \( \approx -13.5 \text{ kcal/mol} \) (estimated by subtracting \( T\Delta S^\circ \) for the first binding from the total \( T\Delta S^\circ \) for the trivalent binding). If this value is correct, where does it come from? A review of the contributors to the entropic loss of binding of \( V \) to \( L \) suggests clues to its origin.

Williams et al. have carefully examined the entropic loss of binding of N-Ac-d-Ala-d-Ala to vancomycin and ristocetin A (a vancomycin group antibiotic). In this semiquantitative analysis, they dissected TAS° for binding of V to N-Ac-d-Ala-d-Ala into three major terms (eq 15): loss of translation and rotation due to a bimolecular association (\(\Delta S^{\circ}_{\text{trans-rot}}\), \(\approx 17\) kcal/mol), the freezing out of four rotors of the peptide (\(\Delta S^{\circ}_{\text{rotors}}\), \(\approx -5\) kcal/mol), and the release of water (\(\Delta S^{\circ}_{\text{solv}}\), \(\approx 19\) kcal/mol). The predicted value of TAS° is close to the experimental value in this system (\(-4.1\) kcal/mol).

\[
\Delta S^{\circ} = \Delta S^{\circ}_{\text{trans-rot}} + \Delta S^{\circ}_{\text{rotors}} + \Delta S^{\circ}_{\text{solv}}
\]

Using analogous reasoning, we estimated the entropic loss in the two intramolecular binding steps for R\(V_3\) and R\(L_3\). We estimate the total entropic loss for the two intramolecular binding steps by eq 16, where TAS° conf defines the additional conformational entropy loss in the two intramolecular binding steps. As estimated above, the value of TAS° second+third for the second and third binding steps is approximately \(-13.3\) kcal/mol. We therefore estimate TAS° conf \(-41\) kcal/mol (eq 17).

\[
\Delta S^{\circ}_{\text{second/third}} = 2 \Delta S^{\circ}_{\text{rots}} + 2 \Delta S^{\circ}_{\text{solv}} + \Delta S^{\circ}_{\text{conf}}
\]

This large loss of conformational entropy can partly be rationalized in terms of structures of R\(V_3\) and R\(L_3\). Although R\(V_3\) is fairly rigid, it still contains nine rotors that are frozen upon complexation to R\(L_3\) (Scheme 1). R\(L_3\) is a more flexible molecule, and its complexation to R\(V_3\) freezes, or partly freezes, additional 18 rotors (Scheme 1). Page and Jencks estimated a value of \(-1.2\)–\(-1.5\) kcal/mol per rotor frozen upon complexation. The entropic penalty from freezing out these rotors, (assuming that all are free in the unassociated state, and frozen in the complex), thus would range between 32 and 40 kcal/mol. This range is reasonably close to the value of our estimate of TAS° conf in the two intramolecular binding steps, given the high degree of approximation in this estimation (the entropic loss per rotor frozen obviously is not the same for the cases considered by Page and Jencks and those considered here, nor are all the rotors in R\(V_3\) and R\(L_3\) the same).

In summary, our analysis of TAS° for the trivalent binding of R\(V_3\) and R\(L_3\) is compatible with (but does not demand) a scheme in which the loss in conformational entropy in two intramolecular bindings offsets the gain in TAS° trans-rot from linking three monomers as trimers. The observation that overall TAS° for the trivalent binding appears to be slightly more than three times of that for binding of V to L is thus, in this analysis, a coincidence.

Conclusions

Polyvalency aims to enhance binding through entropic advantage. The trivalent system we have designed, based on vancomycin and DADA, demonstrates the successful application of this approach, and clarifies some of its principles: this system is the tightest binding one (among relatively low molecular weight organic species) of which we know. Our current understanding of thermodynamics of this trivalent system shows that, as expected, \(\Delta H^F\) for the trimer originates primarily in the enthalpy of association of three V and L groups, and the gains in TAS° trans-rot that come from trivalency are coincidentally largely offset by the loss in conformational entropy of the linking groups on binding.

Aside from its demonstration of a large binding constant, the work carries a prescription for systems in which trivalency might give even larger binding constants. The features in these systems would include (i) rigid receptors and ligands, (ii) conformational stiff linkers, correctly designed to allow receptors and ligands to interact without enthalpic strain and with minimal loss in entropy due to freezing of conformational and rotational terms, and (iii) a large hydrophobic component to binding to give a large positive contribution from TAS from release of water.

Experimental Section

General Methods. The 1H NMR spectra were recorded at 400 MHz. Chemical shifts are reported in parts per million downfield from tetramethylsilane. Vancomycin hydrochloride was purchased from Sigma and used without further purification. Amino acids were purchased from Sigma (St. Louis, Missouri), except for d-Ala-O-4Bu from BACHEM Bioscience (King of Prussia, Pennsylvania). The peptide coupling reagent HBTU was purchased from Applied Biosystems (Atlanta, Georgia). Dimethylformamide (DMF) and dimethyl sulfoxide (DMSO) were dried overnight over silica gel and 4 Å molecular sieves, respectively, followed by distillation under reduced pressure. Diisopropylethylamine (DIEA) was distilled from n-hexane. The monomeric peptide ligand diacetyl-1-lysoyl-d-alanine (L) was available from a previous study.

tert-Butyl 4-Aminobenzylamine Carboxylate. To a solution of 4-aminobenzylamine (3.66 g, 30 mmol) in 60 mL of acetone solution was slowly added di-tert-butyl dicarbonate (2.84 g, 15 mmol) in 10 mL of acetone and 6 mL of triethylamine. The reaction was stirred at room temperature for 30 min, and the solvent was removed by rotary evaporation. The residue was purified by flash chromatography (eluting with 2:3 hexane/ethyl acetate) to give 2.67 g (12 mmol, 80%) of the product as a white solid: Rf = 0.43 (1:1 hexane/ethyl acetate); 1H NMR (300 MHz, CDCl3) \(\delta\) 1.45 (s, 9 H, C\(\text{CH}_3\)), 3.65 (s, 2 H, \(\text{NH}_2\)), 4.18 (d, \(J = 5.4\) Hz, 2 H, \(\text{CH}_2\)), 4.73 (t, 1 H, \(\text{NHCO\text{CO}_{2}H}\)), 6.64 (d, \(J = 6.4\) Hz, 2 H, \(\text{CH}_2\)), 7.07 (d, \(J = 8.1\) Hz, 2 H, \(\text{CH}_2\)); HRMS–FAB (M + Na+) calcd for C\(\text{H}_{22}\)\(\text{Na}_1\)\(\text{O}_4\)\(\text{Na}_1\) 245.1266, found 245.1253.

1,3,5-Benzene Tris(tert-butoxycarbonyl)-4-aminomethyl-phenyl-carboxamide. To a solution of tert-butyl 4-aminobenzylamine carboxylate (1.01 g, 4.5 mmol) in 50 mL of dry CHCl\(_3\) was added 1.0 mmol of DIEA and 1.35-benzene tris(carbonyl chloride) (0.40 g, 1.5 mmol) at 0 ℃ under stirring. After 2 h, the reaction mixture was poured into 5 mL of saturated aqueous NaCl solution and extracted with CHCl\(_3\). The solvent was removed by rotary evaporation, and the residue was purified by flash chromatography (eluting with 100:3 CH\(_2\)Cl\(_2\)/methanol) to give 1.01 g (1.2 mmol, 82%) of the product as a white powder: Rf = 0.50 (20:1 CH\(_2\)Cl\(_2)/\text{methanol}); 1H NMR (DMSO-d\(_6\)) \(\delta\) 1.39 (s, 27 H, C\(\text{CH}_3\)), 4.10 (d, \(J = 5.96\) Hz 6 H, \(\text{CH}_2\)), 7.24 (d, \(J = 8.3\) Hz, 3 H, \(\text{CH}_2\)), 7.36 (t, \(J = 6.1\) Hz, 6 H, \(\text{CH}_2\)), 7.72 (d, \(J = 8.2\) Hz, 6 H, \(\text{CH}_2\)), 8.67 (s, 3 H, \(\text{CH}_3\)), 10.55 (s, 3 H, CONH); HRMS–FAB (M + Na+) calcd for C\(\text{H}_{15}\)\(\text{N}_5\)\(\text{Na}_1\)\(\text{O}_3\) 403.85, found 403.35.

1,3,5-Benzene Tris(N-tert-butoxy carbonyl)-4-aminomethyl-phenyl-carboxamide. A solution of 1,3,5-Benzene Tris(N-tert-butoxy carbonyl)-4-aminomethyl-phenyl-carboxamide (170 mg, 0.21 mmol) in 5 mL of 1:1 CH\(_2\)Cl\(_2\)/TFA was stirred at room temperature for 1 h. After the solvent had been removed by rotary evaporation, we recovered 170 mg of a white powder (95%) as tris(trifluoroacetate) salt: 1H NMR (DMSO-d\(_6\)) \(\delta\) 4.02 (q, 6 H, \(\text{CH}_2\)), 7.46 (d, \(J = 8.6\) Hz, 6 H, \(\text{CH}_2\)), 7.83 (d, \(J = 8.6\) Hz, 6 H, \(\text{CH}_2\)), 8.21 (bs, 9 H, \(\text{NH}_3\)), 8.70 (s, 3 H, \(\text{CH}_3\)), 10.71 (s, 3 H, CONH); HRMS–FAB (M + H+) calcd for C\(\text{H}_{38}\)\(\text{O}_8\)\(\text{N}_2\) 523.2458, found 523.2468.

R\(V_3\). To a solution of 100 mg of vancomycin hydrochloride (67 μmol), in 0.5 mL of dry DMSO, were added 0.5 mL of dry DMF and 1,3,5-benzene tris(N-4-aminomethyl-phenoxy-carboxamide) (19 mm, 22 μmol). The mixture was cooled to 0 ℃, and 38 mg (100 μmol) of HBTU was added, followed by 26 mg (206 μmol) of DIEA. The

solution was allowed to warm to room temperature and stirred overnight. Analytical reverse-phase HPLC showed nearly complete loss of vancomycin and appearance of a much less polar major product. Removal of the solvent afforded 130 mg of crude product. Preparative reverse-phase HPLC purification and lyophilization afforded a white foam as the R′V₃ hexa(trifluoroacetate). The ¹H NMR spectrum showed the resonances expected for vancomycin and the hub units \[\text{Dry DMSO-}d₆\] of 4-aminomethylphenyl-carboxamide trifluoroacetate salt (51 mg, 135 \(\mu\)mol). The ESIMS exhibited an ion at \(m/z\) 4818.8 consistent with the calculated average molecular weight of 4817.4 for the parent ion (M+H⁺), \(C_{222}H_{350}N_{13}O_{35}Cl_3\).

R′L₅s. A suspension of 86 mg of \(N^\alpha\)-Ac-L-Lys-d-Ala-d-Ala-OtBu (0.22 mmol) in CH₂Cl₂ was cooled to 0 °C. To this suspension was added 20 mg of 1,3,5-benzene tris(carbonyl chloride) (0.075 mmol) in 2 mL of CH₂Cl₂ in portions. The ice bath was removed, and the solution was stirred under argon for 2 h, and a fine white precipitate formed. Filtration afforded 25 mg of product as white flaky solid (0.019 mmol). The crude tert-butyl ester-protected peptide was then stirred in a 1:1 mixture of TFA/CH₂Cl₂ for 1 h to cleave tert-butyl groups. After removal of the solvent and TFA by rotary evaporation, the final residue was purified by reverse phase HPLC and afforded the desired R′L₅s. \(3^\text{H}\) NMR (DSMO-\(d₆\)) \(\delta\) 4.45 (d, \(CH_2\)NH), 7.28 (d, ArH), 7.74 (d, ArH), 8.70 (s, ArH), 10.60 (s, CONH). \[\text{ESIMS exhibited an ion at m/z} 1658.9\] consistent with the calculation average molecular weight of 1658.5 for the parent ion (M+H⁺), \(C_{212}H_{31}N_{4}O_{6}\) 435.2244, found 435.2221.

**UV Spectrophotometry.** The binding constant for association of R₃V₃ with L was determined by UV difference spectrophotometry, using the method described previously.¹ The data were fit to a simple 1:1 binding model, assuming that the association of L with each site of R₃V₃ is an independent event with the same affinity. A nonlinear least-squares curve fitting routine was used in extracting the binding constant.

**High-Pressure Liquid Chromatography.** HPLC was performed using a Waters 600E or a Rainin Dynamax Model SD-300 HPLC chromatography system with a UV detector using C18 columns from Rainin or VyDAC. A 4.4 mm i.d. column was used for analysis and a 21.4 mm i.d. column was used for preparative separations. Linear gradients of 0.1% TFA in acetonitrile and 0.1% TFA in water were used in HPLC elution. The flow rate for the analytical study was 1.0 mL/min, and 7.5 mL/min for the preparative separation. The injection volume for analytical separation was 20 \(\mu\)L. The parameters in eq 12 were determined as follows. Values of \([L]\) assumed to be constant since L was in excess in the experiments. Values of \([R′L₃]\) and \([R′V₃−R′L₃]\) were estimated from the integrals of their peaks in HPLC. Values of \([R′V₃−3L]\) were estimated from integrals of \(R′V₃\) because \(R′V₃\) dissociated to \(R′V₃\) on the column. Values of \(\nu\) were thus calculated using eq 12. Integrations were performed using Baseline 810, a program provided by Waters, by plotting chromatograms, estimating baselines, and integrating areas of peaks.

**Isothermal Titration Calorimetry.** Calorimetry experiments were carried out using a MicroCal MCS titration calorimeter as described in detail elsewhere.²⁵ Briefly, titrations were performed in 5.0 mM phosphate buffer at pH 7.0, and typically consisted of 3- or 5\(\mu\)L of ligand solution in a schedule of 20 to 30 injections spaced at intervals of 4–5 min with a syringe stirring speed of 500 rpm. The calibrated feedback current (\(\text{mV/s}\)) was recorded as a function of time and was used to determine the heat released following an injection by integration. Heats were normalized to give the enthalpy of binding (\(\Delta H\), kcal/mol). For experiments in which binding constants were determined, the data were analyzed by a single-set-of-sites binding model with MicroCal Origin software. Concentrations of \(R′L₃\) were determined by amino acid analysis.

Acknowledgment. This work was supported in part by the National Science Foundation NSF CHE-9801358, the National Institutes of Health (NIH) Grants GM30367, and GM53210 (to R.M.W.). J.R. thanks Eli Lilly (1996), Hoffman-La Roche (1997), and Glaxo Wellcome (1998) for Predoctoral Fellowships. NMR instrumentation was supported by National Institutes of Health Grant 1 S10 RR4870 and National Science Foundation Grant CHE-88-14019. FAB-Mass spectra were obtained by Dr. Andrew Tyler at Harvard University. ESI-Mass spectra of \(R′V₃\) and \(R′L₅\) and concentrations of \(R′L₅\) solution were obtained by the Harvard MicroChem Facilities.

**Supporting Information Available:** Complete derivation of eq 11 (PDF). This material is available free of charge via the Internet at http://pubs.acs.org.